

Oblique Triangles Practice

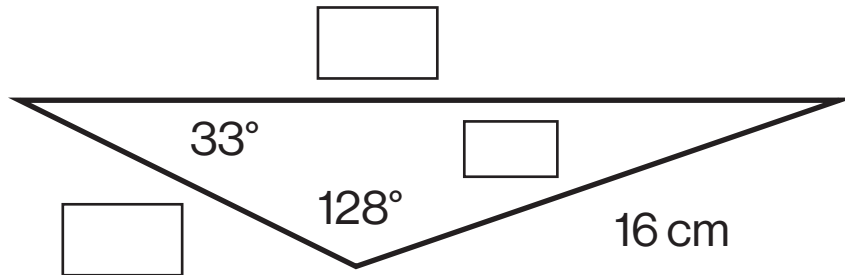
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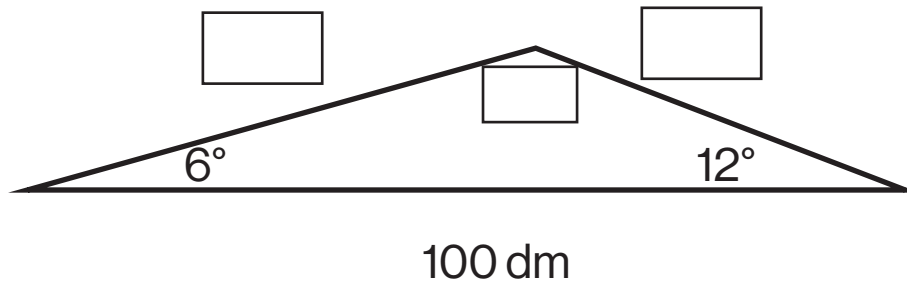
Question 1

Determine the unknown values (round to the nearest tenth)

I.



II.



Question 2

Based on the data, determine if the information belongs to one triangle, two triangles, or no triangle. Then, solve for the unknown values if possible (round to the nearest whole number)

I.

$A = 40^\circ$

$a = 54\text{ yd}$

$b = 62\text{ yd}$

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II. $A = 75^\circ$ $a = 52 \text{ yd}$ $b = 72 \text{ yd}$

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III. $A = 43^\circ$

$a = 81 \text{ yd}$

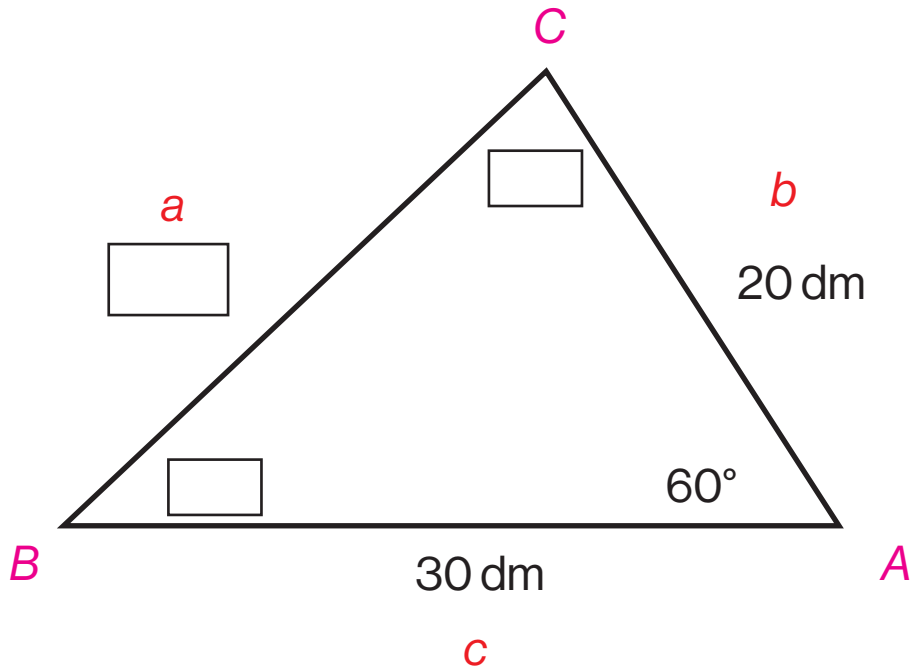
$b = 62 \text{ yd}$

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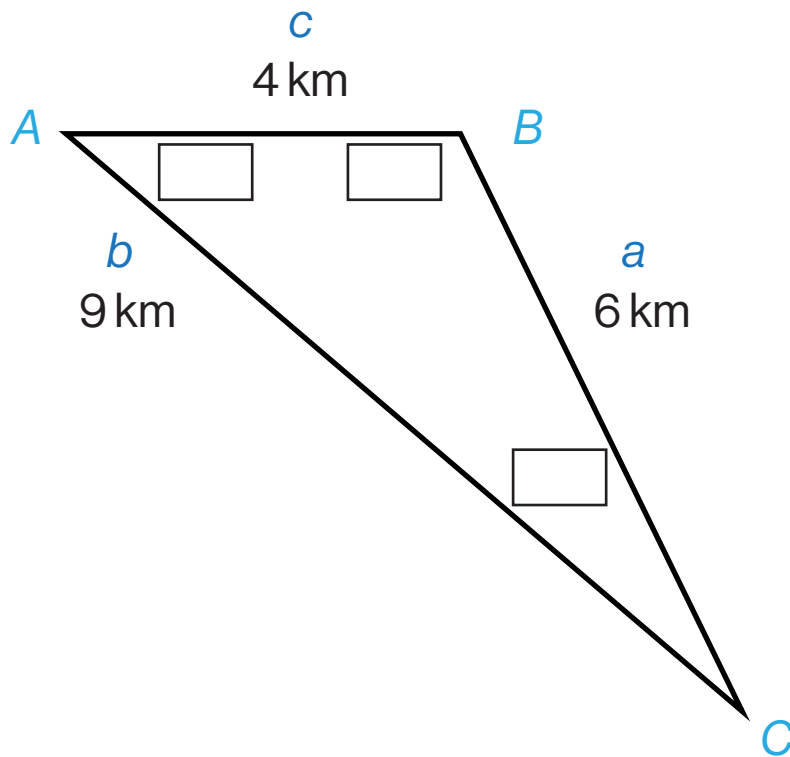
Question 3

Determine the unknown values (round to the nearest tenth)

I.



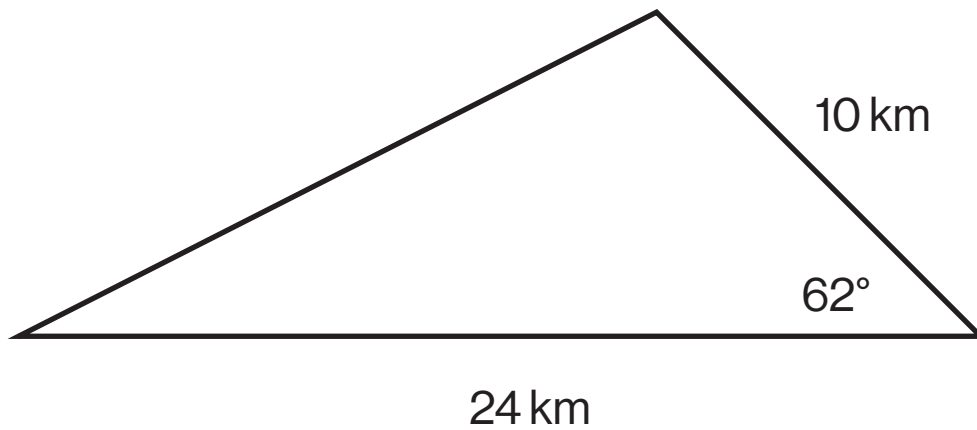
II.



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Question 4

Determine the area of the triangle (round to the nearest whole number)



Oblique Triangles Practice

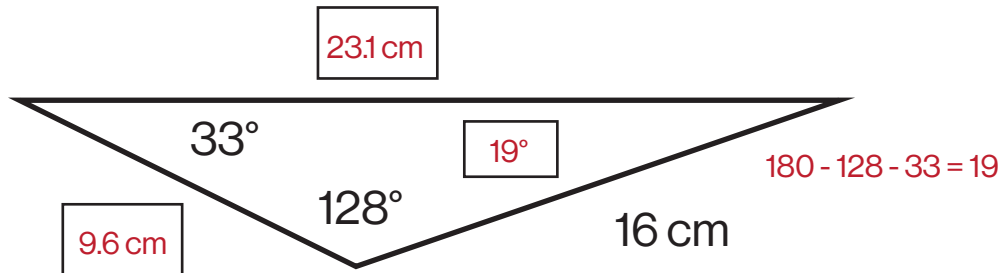
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Date: _____

Question 1

Determine the unknown values (round to the nearest tenth)

I.



$$\frac{x}{\sin(128^\circ)} = \frac{16}{\sin(33^\circ)}$$

$$x \cdot \sin(33^\circ) = 16 \cdot \sin(128^\circ)$$

$$x = \frac{16 \cdot \sin(128^\circ)}{\sin(33^\circ)}$$

$$23.1 \approx \frac{16 \cdot \sin(128^\circ)}{\sin(33^\circ)}$$

$$\frac{x}{\sin(19^\circ)} = \frac{16}{\sin(33^\circ)}$$

$$x \cdot \sin(33^\circ) = 16 \cdot \sin(19^\circ)$$

$$x = \frac{16 \cdot \sin(19^\circ)}{\sin(33^\circ)}$$

$$9.6 \approx \frac{16 \cdot \sin(128^\circ)}{\sin(33^\circ)}$$

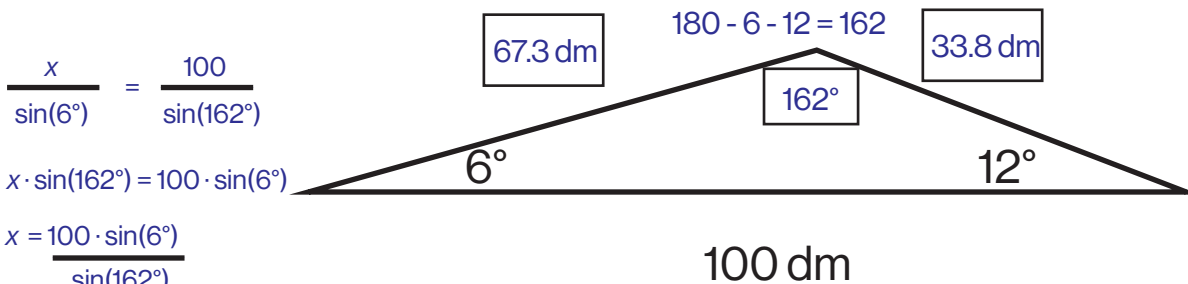
$$\frac{x}{\sin(12^\circ)} = \frac{100}{\sin(162^\circ)}$$

$$x \cdot \sin(162^\circ) = 100 \cdot \sin(12^\circ)$$

$$x = \frac{100 \cdot \sin(12^\circ)}{\sin(162^\circ)}$$

$$67.3 \approx \frac{100 \cdot \sin(12^\circ)}{\sin(162^\circ)}$$

II.



$$\frac{x}{\sin(6^\circ)} = \frac{100}{\sin(162^\circ)}$$

$$x \cdot \sin(162^\circ) = 100 \cdot \sin(6^\circ)$$

$$x = \frac{100 \cdot \sin(6^\circ)}{\sin(162^\circ)}$$

$$33.8 \approx \frac{100 \cdot \sin(6^\circ)}{\sin(162^\circ)}$$

Question 2

Based on the data, determine if the information belongs to one triangle, two triangles, or no triangle.

Then, solve for the unknown values if possible (round to the nearest whole number)

I. $A = 40^\circ$

$a = 54 \text{ yd}$

$b = 62 \text{ yd}$

$$\frac{62}{\sin(B^\circ)} = \frac{54}{\sin(40^\circ)}$$

$$54 \cdot \sin(B^\circ) = 62 \cdot \sin(40^\circ)$$

$$\sin(B^\circ) = \frac{62 \cdot \sin(40^\circ)}{54}$$

$$(B^\circ) = \sin^{-1}\left(\frac{62 \cdot \sin(40^\circ)}{54}\right)$$

$$(48^\circ) \approx \sin^{-1}\left(\frac{62 \cdot \sin(40^\circ)}{54}\right)$$

180° Check:

$$B1: 48^\circ \quad B2: 180^\circ - 48^\circ = 132^\circ$$

$$A + B1: 40^\circ + 48^\circ = 88 < 180 \quad \checkmark$$

$$A + B2: 40^\circ + 132^\circ = 172 < 180 \quad \checkmark$$

both pass = two possible triangles

Remaining Triangle:

$$C1: 92^\circ \quad C2: 8^\circ$$

$$\frac{c1}{\sin(92^\circ)} = \frac{54}{\sin(40^\circ)}$$

$$c1 \cdot \sin(40^\circ) = 54 \cdot \sin(92^\circ)$$

$$c1 = \frac{54 \cdot \sin(92^\circ)}{\sin(40^\circ)}$$

$$84 \approx \frac{54 \cdot \sin(92^\circ)}{\sin(40^\circ)}$$

$$\frac{c2}{\sin(8^\circ)} = \frac{54}{\sin(40^\circ)}$$

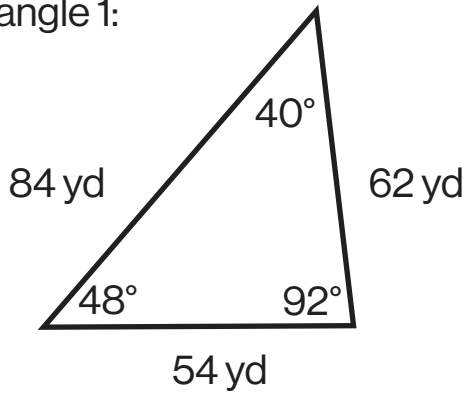
$$c2 \cdot \sin(40^\circ) = 54 \cdot \sin(8^\circ)$$

$$c2 = \frac{54 \cdot \sin(8^\circ)}{\sin(40^\circ)}$$

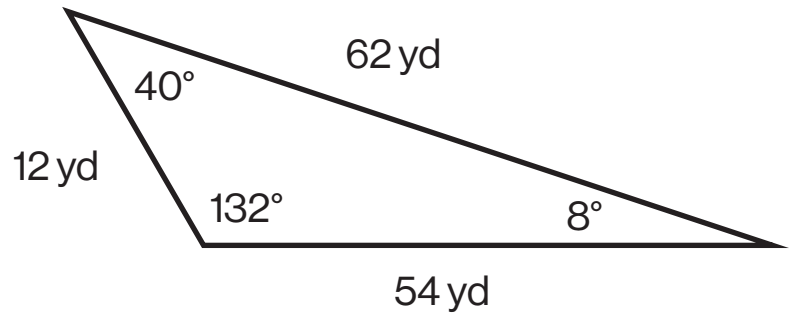
$$12 \approx \frac{54 \cdot \sin(8^\circ)}{\sin(40^\circ)}$$

Oblique Triangles Practice

Triangle 1:



Triangle 2:



II. $A = 75^\circ$ $a = 52$ yd $b = 72$ yd

$$\frac{72}{\sin(B^\circ)} = \frac{52}{\sin(75^\circ)}$$

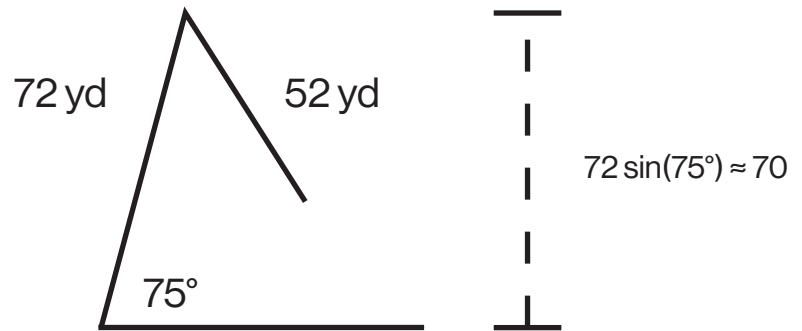
height check:

$$52 \cdot \sin(B^\circ) = 72 \cdot \sin(75^\circ)$$

$$\sin(B^\circ) = \frac{72 \cdot \sin(75^\circ)}{52}$$

$$(B^\circ) = \sin^{-1}\left(\frac{72 \cdot \sin(75^\circ)}{52}\right)$$

$$\text{N/A} = \sin^{-1}\left(\frac{72 \cdot \sin(75^\circ)}{52}\right)$$



$$52 \text{ yd (a)} < 70 \text{ yd (height)}$$

Not a triangle

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III. $A = 43^\circ$ $a = 81 \text{ yd}$ $b = 62 \text{ yd}$

$$\frac{62}{\sin(B^\circ)} = \frac{81}{\sin(43^\circ)}$$

$$81 \cdot \sin(B^\circ) = 62 \cdot \sin(43^\circ)$$

$$\sin(B^\circ) = \frac{62 \cdot \sin(43^\circ)}{81}$$

$$(B^\circ) = \sin^{-1} \left(\frac{62 \cdot \sin(43^\circ)}{81} \right)$$

$$(31^\circ) \approx \sin^{-1} \left(\frac{62 \cdot \sin(43^\circ)}{81} \right)$$

180° Check:

$$B1: 31^\circ \quad B2: 180^\circ - 31^\circ = 149^\circ$$

$$A + B1: 43^\circ + 31^\circ = 74 < 180 \quad \checkmark$$

$$A + B2: 43^\circ + 149^\circ = 192 > 180 \quad \times$$

one pass = one possible triangle

Remaining Triangle:

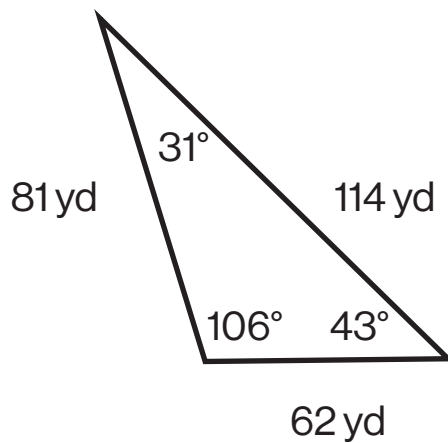
$$C: 106^\circ$$

$$\frac{c}{\sin(106^\circ)} = \frac{81}{\sin(43^\circ)}$$

$$c \cdot \sin(43^\circ) = 81 \cdot \sin(106^\circ)$$

$$c = \frac{81 \cdot \sin(106^\circ)}{\sin(43^\circ)}$$

$$114 \approx \frac{81 \cdot \sin(106^\circ)}{\sin(43^\circ)}$$



Oblique Triangles Practice

Question 3

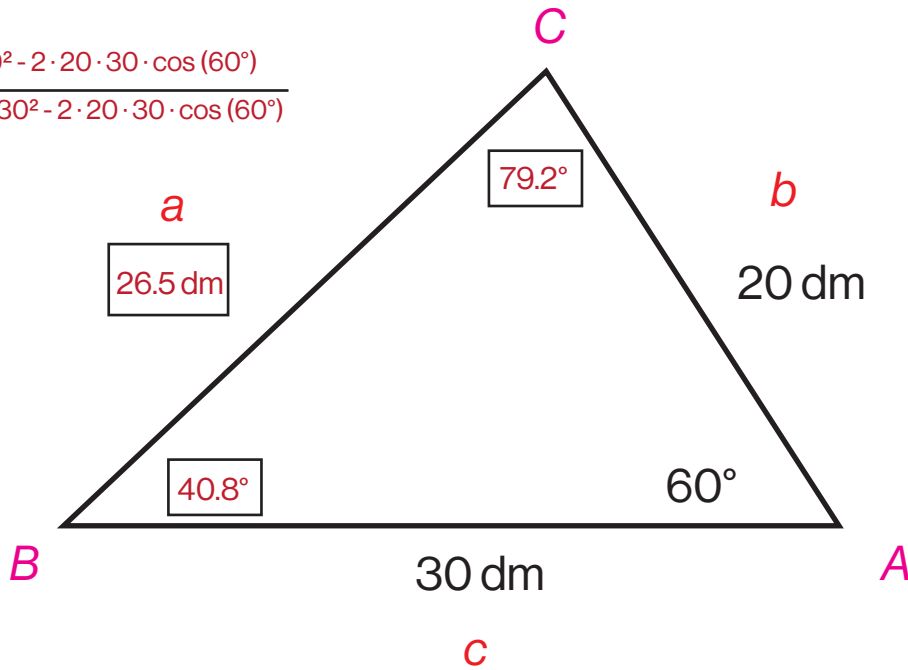
Determine the unknown values (round to the nearest tenth)

I.

$$a^2 = 20^2 + 30^2 - 2 \cdot 20 \cdot 30 \cdot \cos(60^\circ)$$

$$a = \sqrt{20^2 + 30^2 - 2 \cdot 20 \cdot 30 \cdot \cos(60^\circ)}$$

$$a \approx 26.5$$



$$\frac{20}{\sin(B^\circ)} = \frac{26.5}{\sin(60^\circ)}$$

$$26.5 \cdot \sin(B^\circ) = 20 \cdot \sin(60^\circ)$$

$$\sin(B^\circ) = \frac{20 \cdot \sin(60^\circ)}{26.5}$$

$$(B^\circ) = \sin^{-1}\left(\frac{20 \cdot \sin(60^\circ)}{26.5}\right)$$

$$(40.8^\circ) \approx \sin^{-1}\left(\frac{20 \cdot \sin(60^\circ)}{26.5}\right)$$

II.

$$6^2 = 9^2 + 4^2 - 2 \cdot 9 \cdot 4 \cdot \cos(A^\circ)$$

$$36 = 81 + 16 - 72 \cos(A^\circ)$$

$$36 = 97 - 72 \cos(A^\circ)$$

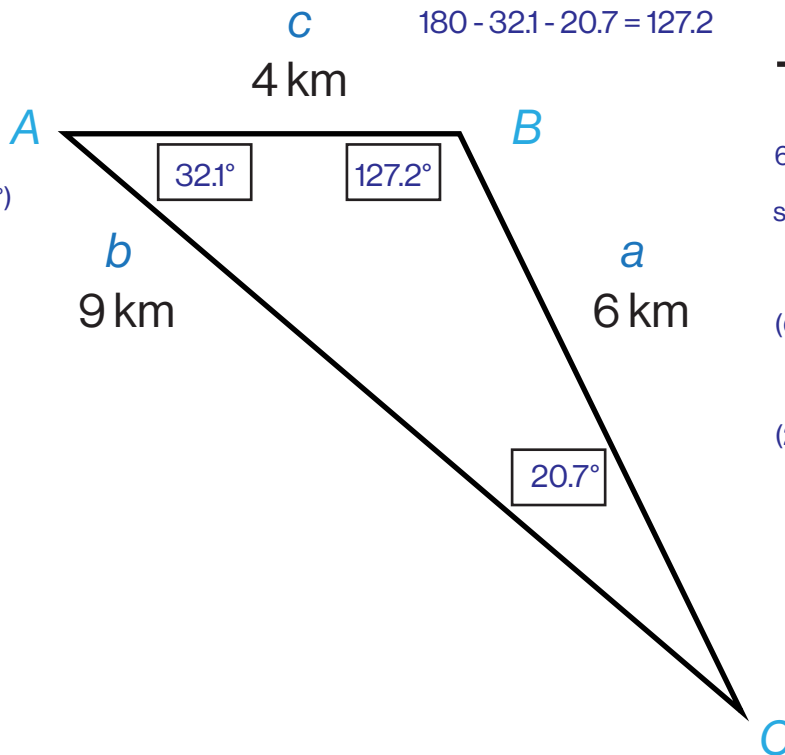
$$-61 = -72 \cos(A^\circ)$$

$$\cos(A^\circ) = \frac{-61}{-72}$$

$$\cos(A^\circ) = \frac{61}{72}$$

$$(A^\circ) = \cos^{-1}\left(\frac{61}{72}\right)$$

$$(32.1^\circ) \approx \cos^{-1}\left(\frac{61}{72}\right)$$



$$180 - 32.1 - 20.7 = 127.2$$

$$\frac{4}{\sin(C^\circ)} = \frac{6}{\sin(32.1^\circ)}$$

$$6 \cdot \sin(C^\circ) = 4 \cdot \sin(32.1^\circ)$$

$$\sin(C^\circ) = \frac{4 \cdot \sin(32.1^\circ)}{6}$$

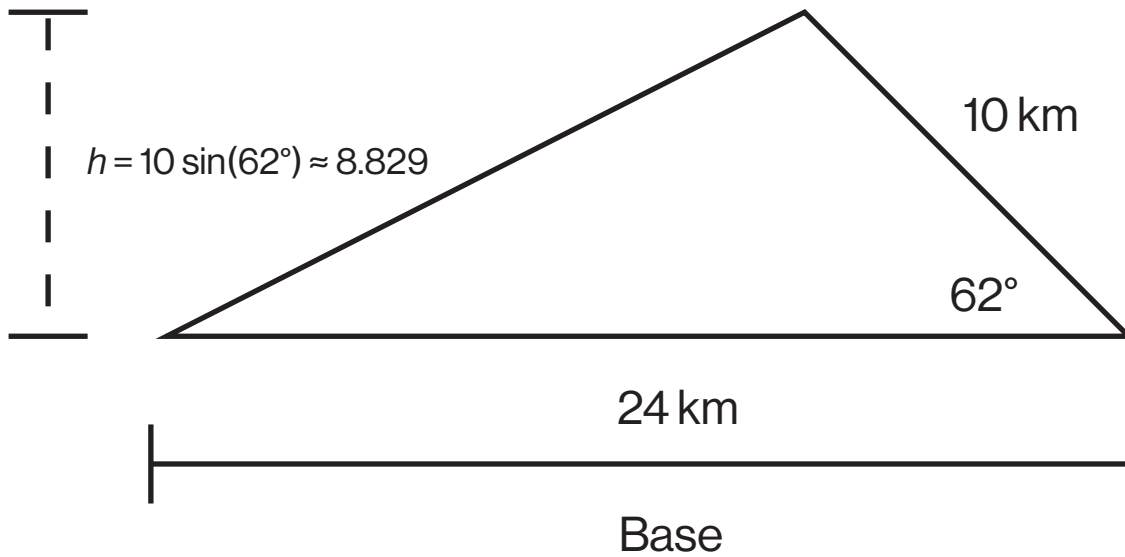
$$(C^\circ) = \sin^{-1}\left(\frac{4 \cdot \sin(32.1^\circ)}{6}\right)$$

$$(20.7^\circ) \approx \sin^{-1}\left(\frac{4 \cdot \sin(32.1^\circ)}{6}\right)$$

Oblique Triangles Practice

Question 4

Determine the area of the triangle (round to the nearest whole number)



$$x = (1/2) \cdot 24 \cdot 8.829 \approx 106$$

$$\text{Area} \approx 106 \text{ km}^2$$